# Vulnerability Analysis of Power Systems Based on Cyber-Attack and Defense Models

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Abstract—Reliable operation of power systems is a primary challenge for the system operators. With the advancement in technology and grid automation, power systems are becoming more vulnerable to cyber-attacks. The main goal of adversaries is to take advantage of these vulnerabilities and destabilize the system. This paper describes a game-theoretic approach to attacker / defender modeling in power systems. In our models, the attacker can strategically identify the subset of substations that maximize damage when compromised. However, the defender can identify the critical subset of substations to protect in order to minimize the damage when an attacker launches a cyber-attack. The algorithms for these models are applied to the standard IEEE-14, 39, and 57 bus examples to identify the critical set of substations given an attacker and a defender budget.

*Index Terms*—Blackouts, Cascading failures, Cyber-attack, SCADA, Smart grid, RTUs, Resilience.

#### I. INTRODUCTION

SMART grids are a result of increasing demand for reliable electric energy. The advancement in the grid's technology is responsible for expanding the capabilities of the traditional power grids generation, transmission, and distribution systems. Technologies such as substation automation, phasor measurement units (PMUs), and advanced metering infrastructures (AMIs) are currently deployed to achieve reliable supply for electric power. However, it increases the cyber component in a smart grid, which potentially increases the attack surface. Furthermore, cyber-attacks are documented as one of the major obstacles towards the reliable power system operation [1], [2]. Attackers take advantage of these technological advancements and launch sophisticated attacks causing severe damage to the systems, e.g., recent blackout of Dec 2015 Ukraine [3].

A power network consists of substations, control centers, AMIs etc. The substations have remote terminal units (RTUs) to monitor and control the field devices such as relays, and circuit breakers. These devices can be remotely manipulated to isolate transmission lines from the network during maintenance or faulty conditions [4] that can result in cascading failures. Therefore, RTUs become the primary target for cyberattacks. The adversary aims to gain complete control of the RTUs and cause severe power system damage by modifying the relay settings, remotely opening circuit breakers, changing measurement data etc. However, the time and effort required in compromising a RTU ensure that an attacker can only access a few RTUs before they are detected [5]. Consequently, strategic attackers try to identify the critical substations to launch a successful attack that maximizes the damage [6].

In order to minimize the damage, defending all the substations simultaneously against cyber-attacks is very difficult given financial budget constraints. Besides, the defense mechanisms become more expensive since dedicated IT professionals are required to continuously monitor the system to identify and patch the vulnerabilities for a stable system operation. Therefore, it becomes necessary to intelligently identify a critical set of substations that can be prioritized and protected to minimize the system damage during an attack.

Previous works [7]–[15] have explored the frameworks and cyber-attack models that could simulate and analyze specific type of cyber-physical vulnerabilities in the power system. A framework for modeling cyber-physical switching attacks and man-in-the-middle attack is presented in [7], [8]. A class of attacks impacting physical processes excluding anomalies in the cyber-domain is referenced in [9]. Data integrity attacks and load redistribution attacks are discussed in [10], [13]. In [11], the impact of cyber-attacks on the transient stability of the system is described. An approach to identify and protect a subset of measurements from the adversaries considering false data injection attacks is presented in [12]. Node overloading attacks due to increasing load resulting in cascading failures are studied in [14]. The above approaches emphasize on specific vulnerabilities but they do not focus on system-wide identification of critical components to attack in a power system. This can provide important insight on which substations and components to protect first for improving the overall system resilience. Moreover, unlike our approach they do not consider a system-wide view on defending against these vulnerabilities especially with limited resource availability.

In this paper, we consider a game-theoretic approach to design an attacker / defender model for power systems. A strategic attacker tries to maximize the damage by identifying the worst-case attack whereas the defender tries to minimize the damage by protecting the critical substations. A worst-case attack refers to an attack on a subset of substations that cause maximum system damage. Here, we consider the cyber-attack on substations to gain access to the RTUs where the adversary can open the circuit breakers by manipulating protection assembly control signals resulting in severe cascading failures. Identifying all the possible attack and defense scenarios is computationally infeasible. Therefore, it is necessary to identify the worst-case attack and defense in an efficient way. The main contributions of the paper are:

· A formal model for an attacker is described, where the cost

of attacking any substation is uniform. In this model, the attacker can identify the critical substations and its components that can be manipulated to disconnect transmission lines from the network that maximize system damage based on the attackers budget.

- An efficient polynomial-time algorithm is presented to identify the worst-case attack based on the attacker model.
- A formal model for a defender is described, where the cost of protecting any substation is uniform. In this model, given a defense budget, a defender can identify the critical substations to protect in order to minimize system damage during a cyber-attack.
- An efficient polynomial-time algorithm is presented to identify the critical substations to defend to minimize damage.
- The case study is performed on the standard IEEE-14, 39, and 57 bus systems [16]. Our results show that the approach captures the worst-case attacks on the power network and effectively uses the defense model to minimize the damage.

The remainder of the paper is organized as follows. Section II presents the attacker model followed by the defender model in Section III. Section IV demonstrates the results. The conclusions are provided in Section V.

## II. SYSTEM MODEL

A power system is a complex network of power generation, delivery, monitoring and control components. The power delivery elements such as transmission lines, buses, and transformers supply power from the generation points to the loads. However, the monitoring and control devices such as protection assemblies and circuit breakers are responsible for isolating faulty elements from the network during abnormal conditions. Due to the advancement in technology, power networks can be remotely controlled using distributed monitoring and control systems i.e., RTUs and SCADA systems.

We consider a power system  $G_p$ , where U is a set of buses, G is a set of generators, T is a set of transformers, L is a set of loads, and P is a set of protection assemblies. The power system is divided into substations. Each substation has its own monitoring and control units referred to as RTUs. Let  $S = \{S^i\}_{i=1}^m$  be the set of substations. Each substation consists of a set of protection assemblies from P. We define  $F(S^i)$  as a function that returns the set of protection assemblies in a substation  $S^i$ . Clearly, the union of all the protection assemblies in every substation represents the set of protection assemblies in the power network, that is,  $\bigcup_{i=1}^m F(S^i) = P$ .

# III. ATTACKER MODEL

In this section, we provide the attacker model that could result in maximum load loss in a power network.

#### A. Worst-Case Attack

The goal of the malicious attacker is to destabilize the power system and maximize the load loss. The attacker achieves this by gaining access to a subset of substations  $S' \subseteq S$ . The adversary is resource bounded, i.e., it can compromise at most  $B_S$  substations. Then, the attacker identifies the protection

assemblies  $P'\subseteq F(S')$  that will be manipulated to isolate transmission lines from the power network. Here, the attacker manipulates at most  $B_P$  protection assemblies. The budget  $B_P$  can represent the maximum number of protection assemblies that the attacker can attack due to a stealthiness criterion. Note that a non-strategic attacker may choose a large  $B_P$  and potentially attack all the protection assemblies within the compromised substations, however, a more strategic attacker may favor a small  $B_P$  as the attack may remain undetected for a longer period of time, which could potentially cause more damage. Also, note that manipulating all the protection assemblies of a substation to isolate power lines may not lead to cascading failures resulting in severe load loss due to the reduction in overall system load. We define the attack on a set of substations S' and protection assemblies P' by  $A_P$ .

Let the loads in the power network be defined by  $L_j$  and current flowing through each load is given by  $I_j$ , where j = 1 to  $n, n \in \mathbb{N}$ . Now, the load loss function is computed as below:

$$J(A_P) = \frac{\sum_{j=1}^{n} L_j}{L_T} \times 100, \ \forall I_j = 0$$
 (1)

where  $L_T$  is the total system load and  $A_P$  is the attack. The problem is formally defined below.

Problem 1 (Worst-Case Attack): Given a power system network  $G_p$ , a substation budget  $B_S$ , and a protection assembly budget  $B_P$ , find a worst-case attack  $A_P$  that maximizes the load loss in the power system network. Formally,

$$\underset{S'}{\operatorname{argmax}} \max_{P' \subseteq F(S')} J(A_P)$$

$$s.t. \quad |S'| \le B_S, \quad |P'| \le B_P$$

# B. Algorithm for Finding Worst-Case Attack

Using exhaustive search to identify worst-case attack is computationally infeasible due to the search space explosion. Hence, we present an efficient Algorithm 1 to find the worstcase attack. The algorithm starts with an empty set and intelligently selects the critical substations one-by-one that cause maximum system damage. Next, from the selected substations, the algorithm iteratively identifies the protection assemblies to manipulate. It takes as input the power system model  $G_p$ , the substation budget  $B_S$ , the protection assembly budget  $B_P$ , and the substation and its component information  $\bar{S}_P$ . Here, substation components refer to the protection assemblies of the substation. Then, it finds the worst-case attack by identifying the critical substations  $S_w$  to compromise, the transmission lines  $T_w$  corresponding to the protection assemblies that are manipulated to be removed from the network, and the resulting load loss  $L_w$ . The substation and its components i.e., protection assemblies is denoted by  $\bar{S}$ , which represents a hash table. At each iteration p, based on  $S_w$ ,  $\bar{S}$  is obtained by using Substation\_comps(). If  $S_w$  is non-empty, the function selects the substations  $S_w$  from the power system that cause maximum load loss in the previous iteration and uses it to obtain a new set of substations to select from that may result in maximum damage in the current iteration p. For each  $s \in \bar{S}$ ,

## Algorithm 1 Algorithm for Finding Worst-Case Attack

```
1: Input: G_p, B_S, B_P, \bar{S}_P
       Initialize: L_w \leftarrow 0, T_w \leftarrow \emptyset, S_w \leftarrow \emptyset, L_g \leftarrow 0
      for p = 1, \ldots, B_S do
             \begin{array}{c} P\\ \text{if } S_w = \emptyset \text{ then}\\ \bar{S} \leftarrow \texttt{Substation\_comps}(\bar{S}_P, \emptyset) \end{array}
 4:
  5:
  6:
  7:
                   \bar{S} \leftarrow \texttt{Substation\_comps}(\bar{S}_P, S_w)
  8:
             for all s \in \bar{S} do
  9.
                   P_t \leftarrow F(s)
10:
                   T_P, L_P \leftarrow \texttt{Worst\_Attack}(G_p, P_t, B_P)
11:
12:
                   if L_P > L_w then
                         \hat{L}_w \leftarrow L_P, T_w \leftarrow T_P, S_w \leftarrow s
13:
                        if (L_g - L_w) \le \varepsilon then
14:
15:
                         end if
16:
17:
                        else:
18:
                   end if
19.
20:
             end for
21: end for
22: return S_w, T_w, L_w
```

Worst\_Attack $(G_p,P_t,B_P)$  computes and returns the transmission line outages corresponding to the selected protection assemblies and load loss denoted by  $T_P,\,L_P$  respectively that cause maximum damage. In each iteration p, if  $L_P>L_w$  then the solution is updated. The loop terminates if no further improvement  $L_q-L_w$  is observed in the next iteration p.

The function Worst\_attack() is described as Algorithm 2. The algorithm intelligently selects the critical protection assemblies one-by-one to isolate transmission lines that cause maximum load loss (equation 1). It takes as input the power system model  $G_p$ , substation components  $P_t$ , and the protection assembly budget  $B_P$ . Further, it identifies the maximum load loss  $L_{w}^{'}$  and the outages  $T_{w}^{'}$ . The algorithm starts with an empty set and uses  $Max_{loss}(G_p, P_t, \emptyset)$  to identify the component outages resulting in maximum damage. This function simulates a set of contingencies, i.e., outages of components and returns the one that cause maximum load loss. The component is represented by  $T_P$  and the load loss caused by the component is represented by  $L_P^{'}$ . For each iteration i, Updated\_comps $(P_t, T_P^{'})$  uses  $T_P^{'}$  and returns a new set of components  $\hat{P}_t$  to be removed from  $G_p$  depending upon  $B_P$ .  $\hat{P}_t$  represents a list of contingencies that are needed to be simulated. Next, Max\_loss $(G_p, P_t, \hat{P}_t)$  uses the updated

# Algorithm 2 Worst Attack() Function

```
1: Input: G_p, P_t, B_P

2: Initialize: L_w' \leftarrow 0, T_w' \leftarrow \emptyset

3: T_P', L_P' \leftarrow \text{Max\_loss}(G_p, P_t, \emptyset)

4: L_w' \leftarrow L_P', T_w' \leftarrow T_P'

5: for i = 1, \dots, B_P do

6: \hat{P}_t \leftarrow \text{Updated\_comps}(P_t, T_P')

7: T_P', L_P' \leftarrow \text{Max\_loss}(G_p, P_t, \hat{P}_t)

8: if L_P' > L_w' then

9: L_w' \leftarrow L_P', T_w' \leftarrow T_P'

10: end if

11: end for

12: return T_w', L_w'
```

component list  $\hat{P}_t$  to identify the maximum load loss causing components in the current iteration i. In each iteration i, if the load loss  $L_P'$  is greater than the maximum load loss  $L_w'$  then the solution is updated. The worst-case running time of Algorithm 1 is  $O(|S| \times |B_S| \times |P| \times |B_P|)$ , which is non-exponential.

#### IV. DEFENDER MODEL

In this section, we provide the defender model to improve the power system resilience by minimizing the load loss. Here, based on the attack on the substations and its components, a set of critical substations to be protected is identified.

### A. Defender's Problem

The goal of the defender is to improve the system resilience and minimize the load loss possible. A defender achieves this by protecting a subset of substations  $D_S$  from the total number of substations S, i.e.,  $D_S \subseteq S$ . The defender is resource bounded, i.e., it can protect at most  $B_D$  substations. The substations can be protected using various methods such as better firewall protection against intrusion, application whitelisting, network segmentation [17]. Note that this model can provide important insight upon which substations can be upgraded first considering financial budget constraints and the worst-case attack. The problem is formally defined below.

Problem 2 (Defender's Problem): Given a power system  $G_p$  and a defense budget  $B_D$ , find a defense strategy  $D_P$  that minimizes the load loss in the power network. Formally,

$$\underset{D_{S}}{\operatorname{argmin}} \max_{S^{'} \subseteq S - D_{S}} \max_{P^{'} \subseteq F(S^{'})} J(A_{P})$$

$$s.t. \quad |D_{S}| \leq B_{D}, \quad |S^{'}| \leq B_{S}, \quad |P^{'}| \leq B_{P}$$

#### B. Algorithm for Finding the Critical Substations to Protect

Using exhaustive search to identify the critical substations to protect is computationally infeasible due to the search space explosion. Hence, we present an efficient Algorithm 3 to find the set of critical substations to protect. The algorithm starts with an empty set and intelligently selects the critical substations one-by-one to protect that minimizes system damage. It takes the power system model  $G_p$ , the substation budget  $B_S$ , the protection assembly budget  $B_P$ , and the defense budget  $B_D$  as inputs. Further, it identifies the critical substations  $S_D$  to be protected to minimize the load loss during an attack.

First, the worst-case attack with no defense is obtained using  $\mathtt{Get\_Attack}(G_p, B_S, B_P, \emptyset, \emptyset)$ , which is same as Algorithm 1. It provides the substations  $\hat{S}_w$  to compromise that maximizes the damage. From the identified worst-case attack, the substation to be protected is identified using  $\mathtt{Get\_Attack}(G_p, B_S, B_P, S_D, s)$ . This function is similar to Algorithm 1 but the only difference is that it computes the worst-case attack after removing the substations to be protected  $S_D$  and the substations s that belongs to  $\hat{S}_w$  from the attackers list of attackable substations. For each iteration s and for each  $s \in \hat{S}_w$ , the substation to be protected that minimizes the load loss, i.e., if  $\hat{L}_w < L_w$  is identified and the solution is

## Algorithm 3 Algorithm to Find Critical Substations to Protect

```
1: Input: G_p, B_S, B_P, B_D
      Initialize: S_d^{'} \leftarrow \emptyset, S_D \leftarrow \emptyset, L_w \leftarrow 100
      \hat{T}_w, \hat{L}_w, \hat{S}_w \leftarrow \texttt{Get\_Attack}(G_p, B_S, B_P, \emptyset, \emptyset)
      for i=1,\ldots,B_D do
            L_w \leftarrow 100
 5:
 6:
            if S_D \neq \emptyset then
                  \hat{S}_w \leftarrow \texttt{Get\_Attack}(G_p, B_S, B_P, S_D, \emptyset)
 7:
 8:
            end if
 9:
            for all s \in \hat{S}_w do
10:
                  \hat{T}_w, \hat{L}_w, S_{sub} \leftarrow \texttt{Get\_Attack}(G_p, B_S, B_P, S_D, s)
11:
                  if \hat{L}_w < L_w then
12:
                       L_w \leftarrow L_w, S_d \leftarrow s
13:
            end for
14:
15:
            S_D \leftarrow S_D \cup S_d
16: end for
17: return S_D
```

updated, i.e.,  $S_D \leftarrow S_D \cup S_d'$ . Next, for each iteration i, the new set of critical substations to compromise  $\hat{S}_w$  is obtained using  $\mathtt{Get\_Attack}(G_p, B_S, B_P, S_D, \emptyset)$  depending upon  $S_D$ . This function returns the new worst-case attack by considering only the substations that are not protected. The worst-case running time of Algorithm 3 is  $O(|S| \times |B_D| \times |S| \times |B_S| \times |P| \times |B_P|)$ , which is non-exponential.

#### V. EVALUATION

To evaluate the developed algorithms, we apply them to the standard IEEE-14, 39, and 57 bus systems. We used a steady state simulator discussed in [18] for our analysis. First,

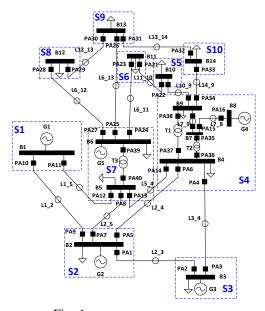


Fig. 1: IEEE-14 Bus System [16]

we discuss an attack-defense scenario for the standard IEEE-14 bus system shown in Figure 1. The blue colored dotted lines represent the substations denoted by S1 , ... , S10. Each transmission line is protected by a pair of protection assembly denoted by PAn, where  $n \in \mathbb{N}$ . These protection assemblies within the substations can be manipulated to open the circuit breakers that can disconnect the transmission lines

from the network to initiate the cascading failures causing severe damage to the power network. Table I shows the details of the performed case study. The attack budget for the system is assumed to be 2. However, the defense budget is increased in steps up to a total of 6 substations. From Table I, it is clear that the load loss for the IEEE-14 bus system is significantly minimized by intelligently selecting the substations to be protected. Moreover, with an increase in the defense budget up to 6 substations a total of 57.31% improvement in load loss is observed. The substations that are attacked and defended are clearly mentioned in the table. Similar results for IEEE-39, 57 bus systems can be obtained using the developed models.

Now, we identify the worst-case attack and defense for the three standard IEEE systems. Figure 2 represents the load loss as a function of various attack and defense budgets. In each figure the x-axis represents the defense budget and the y-axis represents the overall system load loss. Red, green and blue colored markers represent attack budget 2, 3 and 4 respectively. The respective colored markers at the defense budget '0' corresponds to the load loss with no defense. From Figure 2, it is clear that by carefully selecting the substations to be protected and with increase in the defense budget the overall system loss is significantly minimized and the adversary is unable to maximize the damage even with increase in the attack budget. In our analysis, we choose a defense budget of 0-50% of the total number of substations in each system.

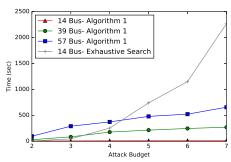


Fig. 3: Attack execution time

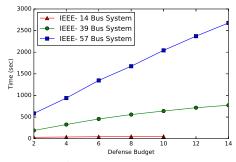
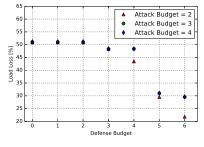


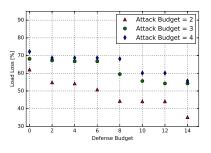
Fig. 4: Defense execution time

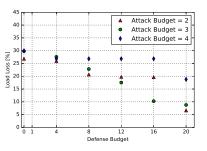
Further, we discuss the time taken to identify the worst-case attack and defense shown in figures 3 and 4 respectively. In each figure, the x-axis represents the attack or defense budget whereas the y-axis represents the time. Red, green and blue lines represent the worst-case attack or defense identification time for IEEE-14, 39, and 57 bus systems respectively. From figure 3, it is clear that as the attack budget increases, the time

TABLE I: IEEE-14 Bus System Attack-Defense Case

Attack Budget	Въ	Defense Budget	Pre-Defense	Post-Defense	Substations	Substations	Improvement
$(B_S)$	$B_P$	$(B_D)$	Load Loss	Load Loss	Attacked	Defended	(%)
2	2	3	51.17	48.30	S7	S4, S3, S2	5.61
2	2	4	51.17	43.46	S1, S6	S4, S3, S2, S7	15.07
2	2	5	51.17	29.55	S8, S9	S4, S3, S2, S7, S6	42.25
2	2	6	51.17	21.84	S5, S10	S4, S3, S2, S7, S6, S9	57.31







(a) IEEE-14 bus system

(b) IEEE-39 bus system

(c) IEEE-57 bus system

Fig. 2: Load loss as a function of various attack and defense budgets for different standard IEEE systems.

taken to obtain the worst-case attack increases very slightly for the three systems. To compare the efficiency of our algorithm, we performed an exhaustive search on IEEE-14 bus system shown by gray colored line in figure 3. It clearly shows that our algorithms perform much better than the exhaustive search and provide the same solution for IEEE-14 bus system as the exhaustive search. Similar analysis can be performed on other systems. Further, figure 4 shows that as the defense budget increases, the time taken to identify the critical set of substations to be protected increases very slowly. It clearly shows that the running time of algorithms 1 and 3 are non-exponential. This execution time is mainly because of the fact that in each iteration of these algorithms, our search is guided intelligently to significantly reduce the search space in order to obtain an efficient and effective solution.

# VI. CONCLUSIONS

The attacker and defender models along with the algorithms to obtain the worst-case attack and defense were developed. The main idea of the attacker model is to select the subset of substations causing maximum system damage when compromised by an adversary. However, the defender model operates to protect the subset of substations which minimize the system damage. The case study on IEEE systems showed how the damage to the power network can be significantly reduced by intelligently selecting a subset of substations to protect, given a defense budget. Under financial budget constraints, prioritizing and protecting the critical substations can greatly increase system resilience. Moreover, these algorithms can be easily applied to larger systems with higher attack and defense budgets. As part of the future work, these models can be applied to changing network topologies to provide online solutions for prioritizing defense resources.

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